

MULTIMEDIA UNIVERSITY

FINAL EXAMINATION

TRIMESTER 3, 2015/2016

EEE 7216 – ENGINEERING OPTIMIZATION

(All Sections / Groups)

2 JUNE 2016

2.30 p.m - 5.30 p.m (3 Hours)

INSTRUCTION TO STUDENT

- 1. This question paper consists of 3 pages only (including this page).
- 2. Attempt ALL FOUR questions. All questions carry equal marks (25 marks) and the distribution of the marks for each question is given.
- 3. Please print all your answers in the Answer Booklet provided.

Question 1

Consider the system of linear equations: (a)

$$x_1 + x_2 + 2x_3 + x_4 = 1 ag{1}$$

$$x_1 - 2x_2 - x_4 = -2 \tag{2}$$

$$x_1, x_2, x_3, x_4 = \{0, 1\}.$$

(i) Rewrite the equations in matrix representation.

[4 marks]

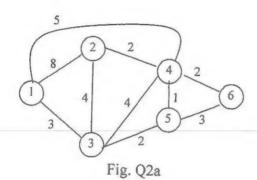
Check if the system has a solution. (ii)

[5 marks]

- Find the optimal solution, if the objective function is to maximize (iii) $f(x) = x_1 + x_2$, subject to constraints (1) and (2). [5 marks]
- As an engineer, you are required to minimize the cost of your concrete mixture that (b) has at least 5 kg of cement, 3 kg of gravel and 4 kg of sand. The information is given below: Mixture A (30% cement, 40% gravel and 30% sand) is RM 5 per kg and Mixture B (10% cement, 20% gravel and 70% sand) is RM 1 per kg.

[11 marks]

Question 2



As a sales engineer, you are required to travel from point 1 to point 6, as illustrated (a) in Fig. Q2a. Suggest a method on how you can derive to the shortest path, illustrate your work clearly. [11 marks]

Continued...

Question 2 (Continued)

- (b) A spring is stretched to length L = 3 cm, 4 cm, 5 cm under applied forces F = 1 N, 2 N, and 4 N respectively. Assuming Hooke's law L = a + bF holds, where a and b are constants.
 - (i) Set up the system of equations to estimate [a, b] using the least square linear approach. [2 marks]
 - (ii) Derive the pseudo inverse of this corresponding matrix.

[6 marks]

(iii) Find the estimate of [a, b].

[6 marks]

Question 3

Consider the following integer linear programing problem:

Maximize $3x_1 + 4x_2$

subject to $7x_1 + 11x_2 \le 88$

 $3x_1 - x_2 \le 12$

and $x_1, x_2 \ge 0$

 x_1, x_2 are integers

(a) Solve the problem graphically.

[10 marks]

(b) Use Branch and Bound method to solve the problem.

[15 marks]

Question 4

Continued...

(a) Consider the following problem:

minimize
$$2x_1 + 3x_2 - 4$$
,

subject to
$$x_1 x_2 = 6$$

$$x_1, x_2 \in \mathbb{R}$$

Use Lagrange's theorem to find all possible local minimizers and maximizers.

[10 marks]

(b) Given the problem to maximize

$$4x_1 + x_2^2$$

Subject to

$$x_1^2 + x_2^2 = 9$$

If the Lagrange condition for the problem is

$$4 + 2\tau x_1 = 0$$
; $2x_2 + 2\tau x_2 = 0$; $x_1^2 + x_2^2 - 9 = 0$;

Use Second Order Sufficient Condition to find the local minimizers and maximizers. [15 marks]

End of Paper.